[L1][CO1][12M

# SIDDARTHA INSTITUTE OF SCIENCE AND TECHNOLOGY:: PUTTUR (AUTONOMOUS)

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### **QUESTION BANK (DESCRIPTIVE)**

**Subject with Code :**Control Systems (19EE0212)

Course & Branch: B.Tech– EEE&ECE

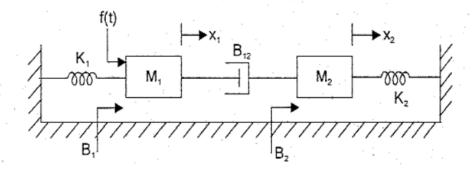
Year & Sem: III-B.Tech & I-Sem

**Regulation:** R19

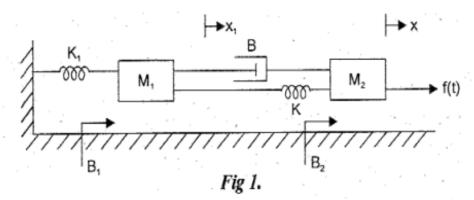
#### UNIT –I

# **SYSTEMS AND REPRESENTATION**

**Q.1** Determine the transfer function,  $\frac{X_1(s)}{F(s)}$  and  $\frac{X_2(s)}{F(s)}$  for the system shown in fig

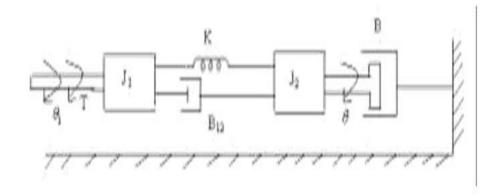


**Q.2** Write the differential equation governing the mechanical system shown in [L1][CO1][12M figure and determine the transfer function



**Q.3** [L1][CO1][12M

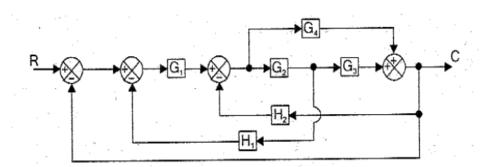
> Write the differential equations governing the mechanical rotational system shown in the figure and find transfer function.



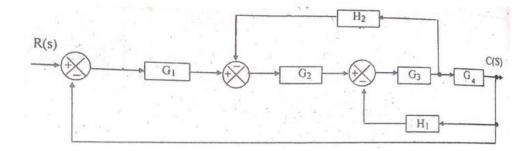
**Q.4** Compare open loop and closed loop control systems based on different [L4][CO1] [8M aspects? a.

> Distinguish between Block diagram Reduction Technique and Signal Flow [L4][CO1][4M]

- b. Graph?
- **Q.5** Using Block diagram reduction technique find the Transfer Function of the [L1][CO1] 12M system.



**Q.6** For the system represented in the given figure, obtain transfer function [L1][CO1] 12M C(S)/R(S).

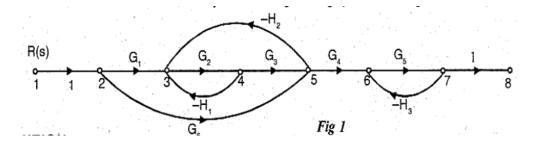


**Q.7** Give the block diagram reduction rules to find the transfer function of the [L4][CO1] 8M system

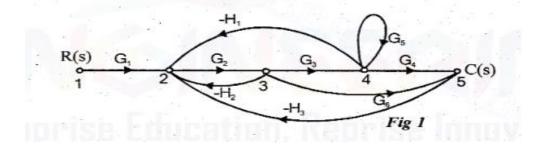
[L4][CO1] 4M

List the properties of signal flow graph.

**Q.8** Find the overall transfer function of the system whose signal flow graph is [L1][CO1] 12M shown below

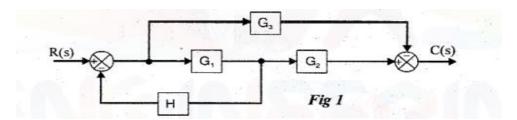


**Q.9** Obtain the overall gain C(S)/R(S) from signal flow graph shown in [L1][CO1] 12M



Q.10 [L1][CO1] 12M

> Convert the block diagram to signal flow graph and determine the transfer function C(S)/R(S).



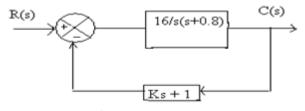
# **UNIT-II** TIME DOMAIN ANALYSIS

[L1,CO2] 12M Q.1 List out the time domain specifications and derive the expressions for Rise time, Peak time and Peak overshoot.

- Q.2 Find all the time domain specifications for a unity feedback control system [L1,CO2] 12M whose open loop transfer function is given by  $G(S) = \frac{25}{S(S+5)}$ .
- A closed loop servo is represented by the differential equation:  $\frac{d^2c}{dt^2} + 8\frac{dc}{dt} = \frac{[L5,CO2]}{2}$ **Q.3** 64e. Where 'c' is the displacement of the output shaft, 'r' is the displacement of the input shaft and e = r - c. Determine undamped natural frequency, damping ratio and percentage maximum overshoot for unit step input.
- Measurements conducted on a servo mechanism, show the system response [L5,CO2] 6M Q.4 to be  $c(t) = 1 + 0.2e^{-60t}$ . 1.2e<sup>-10t</sup> When subject to a unit step input. Obtain an expression for closed loop transfer function, determine the undamped natural frequency, damping ratio?
  - For servo mechanisms with open loop transfer function given below what [L1,CO2] 6M type of input signal give rise to a constant steady state error and calculate their values.

$$G(s)H(s) = \frac{10}{S^2(S+1)(S+2)}$$

- Q.5 A unity feedback control system has an open loop transfer function, G(s) = [L1,CO2] 12M  $\frac{10}{S(S+2)}$ . Find the rise time, percentage overshoot, peak time and settling time for a step input of 12 units.
- Q.6 Define steady state error? Derive the static error components for Type 0, [L1,CO2] 12M Type 1 & Type 2 systems?
- Q.7 A positional control system with velocity feedback shown in figure. What is [L5,CO2] 12M the response c(t) to the unit step input. Given that damping ratio=0.5.Also determine rise time, peak time, maximum overshoot and settling time.



**Q.8** A For servo mechanisms with open loop transfer function given below what [L3,CO2] 6M type of input signal give rise to a constant steady state error and calculate their values.

$$G(s)H(s) = \frac{20(S+2)}{S(S+1)(S+3)}$$

Consider a unity feedback system with a closed loop transfer function  $\frac{C(S)}{R(S)}$  = [L1,CO2] 6M

 $\frac{KS+b}{(S^2+aS+b)}$ . Calculate open loop transfer function G(s). Show that steady state

error with unit ramp

input is given by  $\frac{(a-K)}{h}$ 

Q.9 For a unity feedback control system the open loop transfer function

$$G(S) = \frac{10(S+2)}{S^2(S+1)}$$
.

(i) Determine the position, velocity and acceleration error constants.

[L5,CO2] 6M

(ii) The steady state error when the input is  $\mathbf{R}(\mathbf{S}) = \frac{3}{S} - \frac{2}{S^2} + \frac{1}{3S^3}$ .

[L1,CO2] 6M

- Q.10 What is the characteristic equation? List the significance of characteristic [L1,CO2] 4M equation.
  - The system has  $G(s) = \frac{K}{S(1+ST)}$  with unity feedback where K & T are constant. [L5,CO2] 8M Determine the factor by which gain 'K' should be multiplied to reduce the overshot from 75% to 25%?

# <u>UNIT –III</u>

# **STABILITY ANALYSIS**

Q.1 With the help of Routh's stability criterion find the stability of the [L1,CO3] 12M following systems represented by the characteristic equations:

(a) 
$$s^4 + 8 s^3 + 18 s^2 + 16s + 5 = 0$$
.

(b) 
$$s^6 + 2s^5 + 8s^4 + 12s^3 + 20s^2 + 16s + 16 = 0$$
.

Q.2 With the help of Routh's stability criterion determine the stability of the [L5,CO3] following systems represented by the characteristic equations:

(a) 
$$s^5 + s^4 + 2 s^3 + 2 s^2 + 3s + 5 = 0$$

**(b)** 
$$9s^5 - 20s^4 + 10s^3 - s^2 - 9s - 10 = 0$$

- The open loop Transfer function of a unity feedback control system is [L5,CO3] **Q.3** 12M given by  $G(s)H(s) = \frac{K}{(S+2)(S+4)(S^2+6S+25)}$  Determine the value of K which will cause sustained oscillations in the closed loop system and what is the corresponding oscillation Frequency.
- Q.4 Find the range of K for stability of unity feedback system whose open [L1,CO3] 12M loop transfer function is G(s)  $H(s) = \frac{K}{S(S+1)(S+2)}$  using Routh's stability criterion.
- Q.5 Explain the procedure for constructing root locus.
- [L2,CO3] 12M
- Develop the root locus of the system whose open loop transfer function is **Q.6** [L3,CO3] 12M  $G(s) H(s) = \frac{K}{S(S+2)(S+4)}$ .
- **Q.7** Develop the root locus of the system whose open loop transfer function is [L3,CO3] 12M

**G**(s) **H**(s) = 
$$\frac{K}{S(S^2+4S+13)}$$

**Q.8** Develop the root locus of the system whose open loop transfer function is [L3,CO3] 12M

G(s) H(s) = 
$$\frac{K(S+9)}{S(S^2+4S+11)}$$

Q.9 Develop the root locus of the system whose open loop transfer function is [L3,CO3] 12M

G(s) H(s) = 
$$\frac{K(S^2+6S+25)}{S(S+1)(S+2)}$$

Q.10 Develop the root locus of the system whose open loop transfer function is [L3,CO3] 12M

$$G(s)H(s) = \frac{K}{S(S^2+6S+10)}$$

## **UNIT-IV**

#### FREQUENCY DOMAIN ANALYSIS

Q.1 Develop the Bode plot for the following transfer function [L3,CO4] 12M

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$$G(s)H(s) = \frac{K e^{-0.1s}}{S(S+1) (1+0.1S)}$$

**Q.2** Develop the Bode plot for the system having the following transfer [L3,CO4] 12M function

$$G(s) = \frac{15 (S+5)}{S(S^2 + 16S + 100)}$$

CONTROL SYSTEMS

Define and derive the expression for resonant frequency. **Q.3** a.

[L1,CO4] 6M

Develop the magnitude bode plot for the system having the following

[L3,CO4] 6M

transfer function:

G(s) H(s) = 
$$\frac{2000 (S+1)}{S(S+10) (S+40)}$$

- Q.4 Derive the expressions for resonant peak and resonant frequency and [L3,CO4] 12M hence establish the correlation between time response and frequency response.
- Develop the Bode plot for the following Transfer Function G(s) H(s) =Q.5 [L3,CO4] 12M  $\overline{S^2(0.2S+1)(0.02S+1)}$

From the bode plot determine (a) Gain Margin (b) Phase Margin (c) Comment on the stability

**Q.6** Define and derive the expression for resonant frequency [L1,CO4] 6M

- Given  $\xi = 0.7$  and  $\omega_n = 10$  rad/sec. Find resonant peak, resonant [L5,CO4] 6M frequency and bandwidth.
- Sketch the polar plot for the open loop transfer function of a unity feedback system is [Li 5cnO4] 12M Q.7 by  $G(s) = \frac{1}{S(1+S)(1+2S)}$ . Determine Gain Margin & Phase Margin.
- Sketch the polar plot for the open loop transfer function of a unity feedback system is given CO4] 12M **Q.8** by  $G(s) = \frac{1}{s^{2/(1+S)(1+2S)}}$ . Determine Gain Margin & Phase Margin.
- Draw the Nyquist plot for the system whose open loop transfer function is, Q.9 [L5,CO4] 12M  $G(s)H(s) = \frac{K}{S(S+2)(S+10)}$ . Determine the range of K for which closed loop system is stable.
- Obtain the transfer function of Lead Compensator, draw pole-zero plot and write the 12M Q.10 procedure for design of Lead Compensator using Bode plot.

CONTROL SYSTEMS

# <u>UNIT-V</u>

### STATE SPACE ANALYSIS

- Q.1 Determine the Solution for Homogeneous and Non homogeneous State [L5,CO5] 12M equations
- [L3,CO5] 12M **Q.2** For the state equation:  $\dot{X} = \begin{pmatrix} 0 & 1 \\ -2 & -3 \end{pmatrix} X + \begin{pmatrix} 0 \\ 1 \end{pmatrix} U$  with the unit step input and the initial conditions are  $X(0) = {1 \choose 1}$ . Solve the following (a) State transition matrix
  - (b) Solution of the state equation.
- **Q.3** A system is characterized by the following state space equations:

$$\dot{X}_{1} = -3 x_{1} + x_{2}; \quad \dot{X}_{2} = -2 x_{1} + u; Y = x_{1}$$

- (a) Find the transfer function of the system and Stability of the system.
- (b) Compute the STM
- [L5,CO5] 12M
- [L3,CO5] 8M
- Diagonalize the following system matrix  $A = \begin{pmatrix} 0 & 6 & -5 \\ 1 & 0 & 2 \\ 2 & 2 & 4 \end{pmatrix}$
- A state model of a system is given as:  $\dot{X} = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -6 & -11 & -6 \end{pmatrix} X + \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} U \text{ and } Y = \begin{pmatrix} 1 & 0 & 0 \end{pmatrix} X$

What are the properties of State Transition Matrix.

Determine: (i) The Eigen Values. (ii) The State Transition Matrix.

**Q.6** Find a state model for the system whose Transfer function is given by

G(s) H(s) = 
$$\frac{(7S^2 + 12S + 8)}{(S^3 + 6S^2 + 11S + 9)}$$
 [L3,CO5] 6M

Find the state model of the differential equation is

- [L3,CO5] 6M v + 2v + 3v + 4v = u
- Q.7 [L1,CO5] 12M Diagonalize the following system matrix  $A = \begin{pmatrix} 4 & 1 & -2 \\ 1 & 0 & 2 \\ 1 & -1 & 3 \end{pmatrix}$
- **Q.8** Explain the properties of STM. [L2,CO5] 4M

Q.4

Q.5

[L1,CO5]

[L2,CO5] 12M

4M

b. For the state equation: 
$$\dot{X} = \begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix} X + \begin{pmatrix} 0 \\ 1 \end{pmatrix} U$$
 when,  $X(0) = \begin{pmatrix} 1 \\ 0 \end{pmatrix}$ .

[L1,CO5] 8M

Find the solution of the state equation for the unit step input.

Derive the expression for the transfer function from the state model.

Diagonalize the following system matrix 
$$A = \begin{pmatrix} 0 & 1 & 0 \\ 3 & 0 & 2 \\ -12 & -7 & -6 \end{pmatrix}$$

[L1,CO5] 12M

[L1,CO5] 6M

[L3,CO5] 6M

$$X = Ax + Bu$$
 and  $y = Cx + Du$ 

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